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|----------------------|
| Square Root Function |
|----------------------|

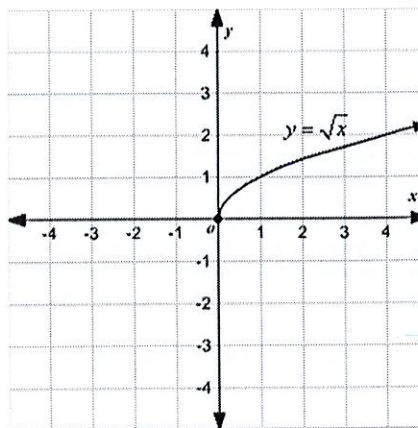
The parent square root function is:

$$y = \sqrt{x}$$

As with all other functions we have learned, square root functions can be transformed.

Key Features of Square Root Functions

Characteristic Points for $y = \sqrt{x}$



Domain:

Range:

Intercept:

Fill in the table below with a description of what happens to the parent function when the following transformations are performed.

| | |
|-----------------|----------------|
| Parent Function | $y = \sqrt{x}$ |
|-----------------|----------------|

| Description | Transformation |
|-------------|--------------------|
| | $y = \sqrt{x + h}$ |
| | $y = \sqrt{x - h}$ |
| | $y = \sqrt{x} + k$ |
| | $y = \sqrt{x} - k$ |
| | $y = -\sqrt{x}$ |
| | $y = a\sqrt{x}$ |

Let's look at the following example.

The graph on the right represents a transformation of the graph of

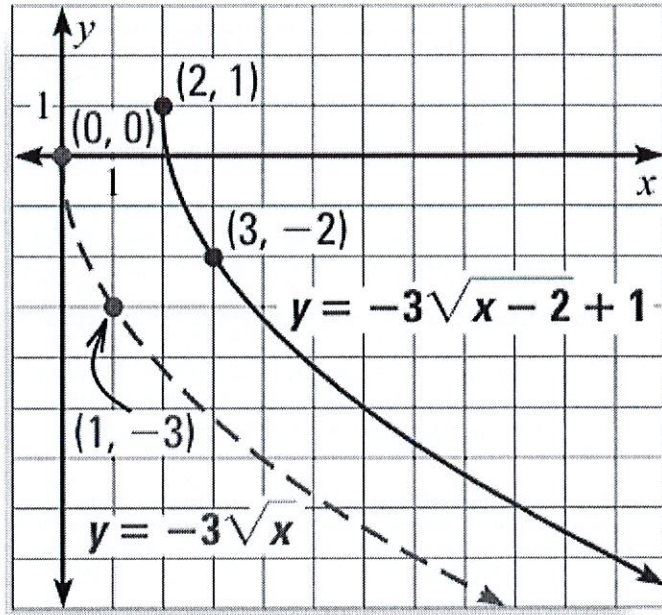
$$y = -3\sqrt{x}$$

The description is as follows:

-
-
-
-

Domain:

Range:



The graph on the right represents a transformation of the graph of

$$y = -3\sqrt{x-2} + 1$$

The description is as follows:

-
-
-
-

Domain:

Range:

TRY NOW

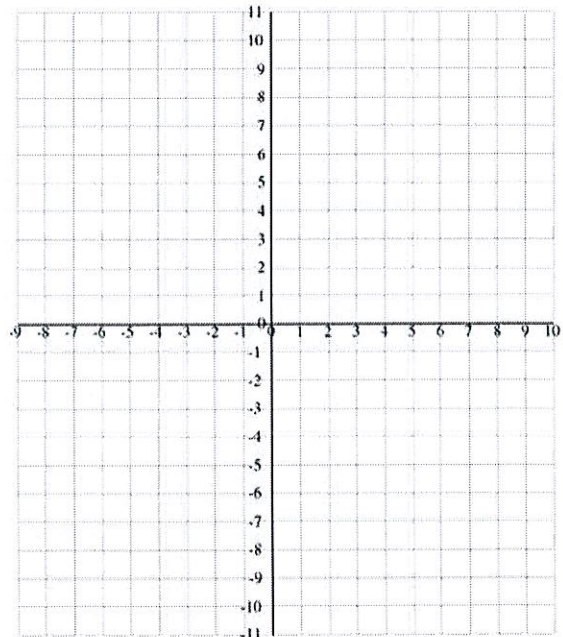
Graph the following function on the graph at right. Describe each transformation, give the domain and and identify any asymptotes.

$$y = 0.5\sqrt{x-3} + 2$$

Description:

Domain:

Range:



range,

| |
|---------------------------|
| Cube Root Function |
|---------------------------|

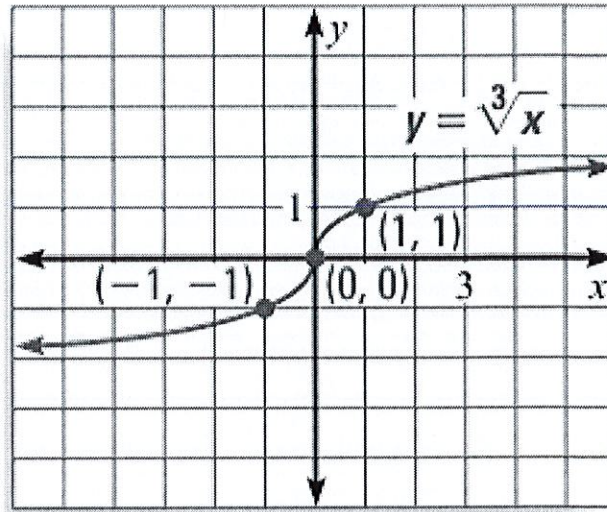
The parent cube root function is:

$$y = \sqrt[3]{x}$$

As with all other functions we have learned, cube root functions can be transformed.

Key Features of Cube Root Functions

Characteristic Points for $y = \sqrt[3]{x}$



Domain:

Range:

Intercept:

Fill in the table below with a description of what happens to the parent function when the following transformations are performed.

| | |
|-----------------|-------------------|
| Parent Function | $y = \sqrt[3]{x}$ |
|-----------------|-------------------|

| Description | Transformation |
|-------------|-----------------------|
| | $y = \sqrt[3]{x + h}$ |
| | $y = \sqrt[3]{x - h}$ |
| | $y = \sqrt[3]{x} + k$ |
| | $y = \sqrt[3]{x} - k$ |
| | $y = -\sqrt[3]{x}$ |
| | $y = a\sqrt[3]{x}$ |

Let's look at the following example.

The graph on the right represents a transformation of the graph of

$$y = 3\sqrt[3]{x}$$

The description is as follows:

Domain:

Range:

The graph on the right represents a transformation of the graph of

$$y = 3\sqrt[3]{x + 2} - 1$$

The description is as follows:

Domain:

Range:

Now it's your turn to find key features and translate logarithmic functions.

TRY NOW

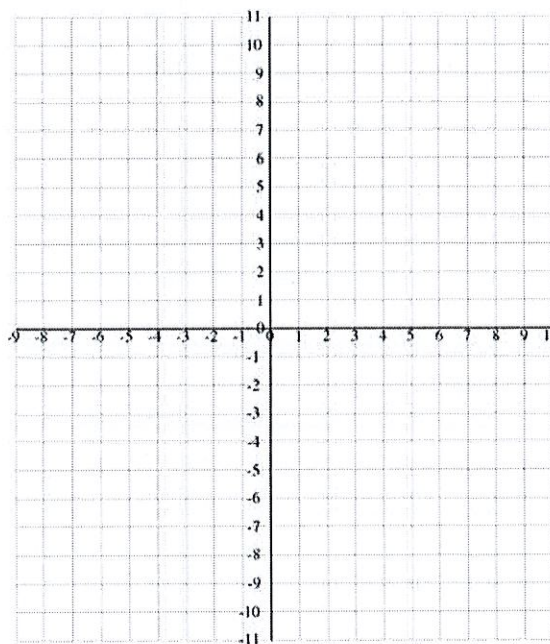
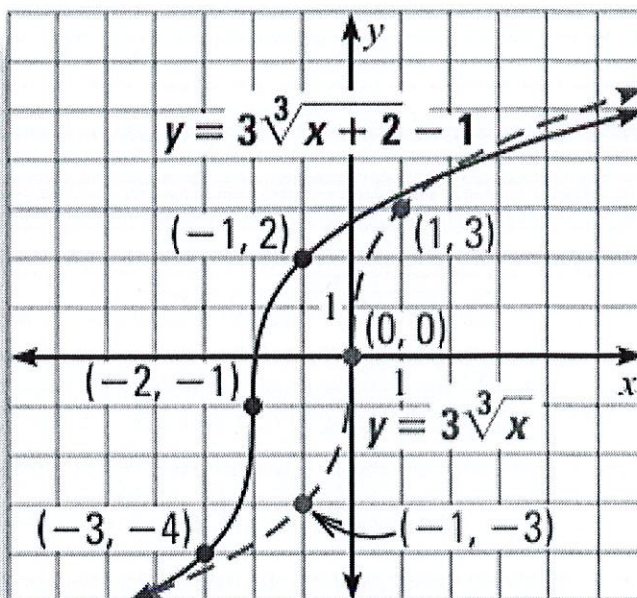
Graph the following function on the graph at right. Describe each transformation, give the domain and and identify any asymptotes.

$$y = 0.5\sqrt[3]{x - 1} + 3$$

Description:

Domain:

Range:



range,

Name _____

Graphing Square and Cube Root Functions

Identify the domain and range of each. Then sketch the graph.

1) $y = \sqrt{x + 4}$

2) $y = -\sqrt{x - 3}$

3) $y = 3 + \sqrt{x + 3}$

4) $y = -\sqrt{x - 1} - 3$

5) $y = \sqrt{x}$

6) $y = \sqrt{x - 2} + 1$

7) $y = \sqrt{x - 1}$

8) $y = \sqrt{x - 2} + 2$

9) $y = 3 + \sqrt{x - 2}$

10) $y = \sqrt{x + 4}$

11) $y = -5 + \sqrt[3]{x}$

12) $y = \sqrt[3]{x - 3}$

13) $y = \sqrt[3]{x + 4}$

14) $y = \sqrt[3]{x + 4}$

15) $y = \sqrt[3]{x + 3}$

16) $y = \sqrt[3]{x - 2} - 3$

17) $y = \sqrt[3]{x + 3} - 1$

18) $y = \sqrt[3]{64x}$

19) $y = \sqrt[3]{x + 5}$

20) $y = 2\sqrt[3]{x - 4}$

| |
|-------------------------|
| Absolute Value Function |
|-------------------------|

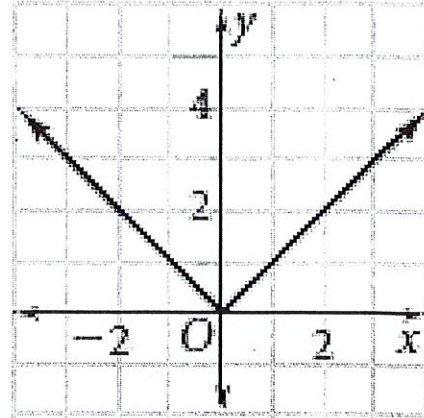
The parent Absolute Value function is:

$$y = |x|$$

As with all other functions we have learned, Absolute value functions can be transformed.

Key Features of Absolute Value Functions

Characteristic Points for $y = |x|$



Domain:

Range:

Intercept:

Fill in the table below with a description of what happens to the parent function when the following transformations are performed.

| | |
|-----------------|-----------|
| Parent Function | $y = x $ |
|-----------------|-----------|

| Description | Transformation |
|-------------|----------------|
| | $y = x + h $ |
| | $y = x - h $ |
| | $y = x + k$ |
| | $y = x - k$ |
| | $y = - x $ |
| | $y = a x $ |

Let's look at the following example.

The graph on the right represents a transformation of the graph of

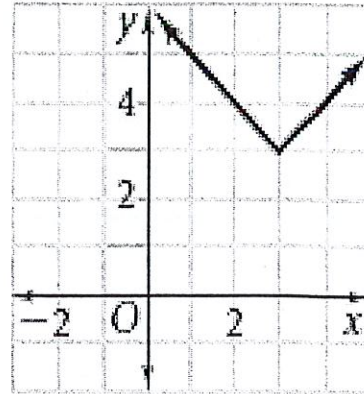
$$y = |x - 3| + 3$$

The description is as follows:

-
-
-
-

Domain:

Range:



TRY NOW

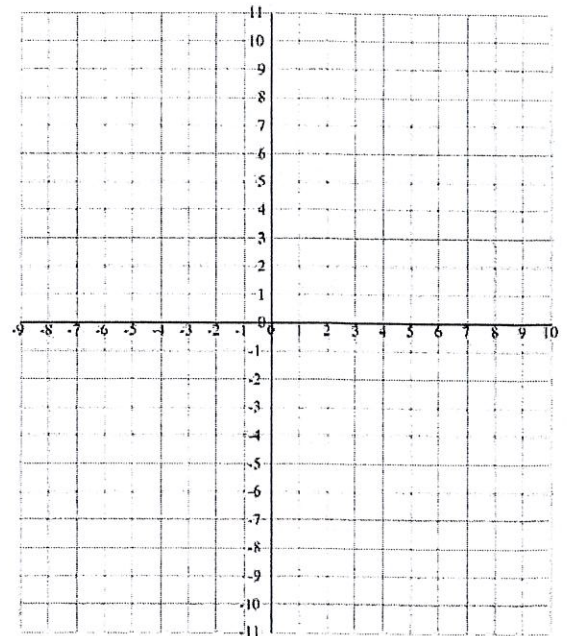
Graph the following function on the graph at right. Describe each transformation, give the domain and range, and identify any asymptotes.

$$y = 2|x + 2| - 5$$

Description:

Domain:

Range:



Practice 2-6

Vertical and Horizontal Translations

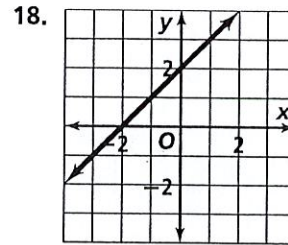
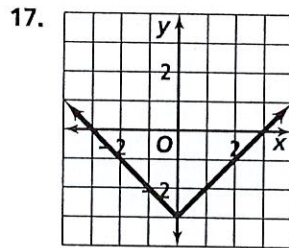
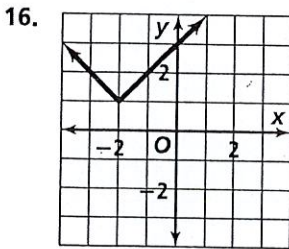
Describe each translation of $f(x) = |x|$ as vertical, horizontal, or diagonal. Then graph each translation.

- | | | |
|-------------------------------|--|--|
| 1. $f(x) = x + 2 $ | 2. $f(x) = x + 4 $ | 3. $f(x) = x - 5$ |
| 4. $f(x) = x + 1 - 1$ | 5. $f(x) = x - 2 + 1$ | 6. $f(x) = \left x - \frac{3}{2}\right $ |
| 7. $f(x) = x - \frac{1}{3}$ | 8. $f(x) = \left x - \frac{5}{2}\right $ | 9. $f(x) = \left x + \frac{1}{2}\right + \frac{3}{2}$ |

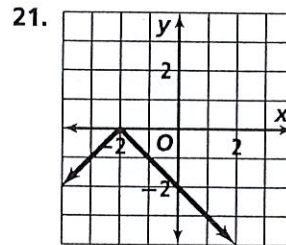
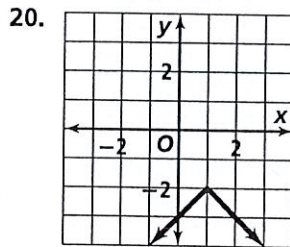
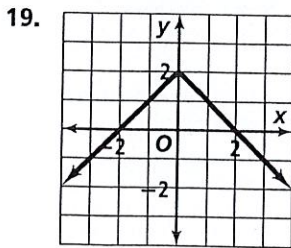
Write an equation for each translation.

- | | |
|--|---|
| 10. $y = x $, 1 unit up, 2 units left | 11. $y = x $, 4 units right |
| 12. $y = - x $, 3 units up, 1 unit right | 13. $y = - x $, $\frac{3}{2}$ units down, $\frac{1}{2}$ unit right |
| 14. $y = x $, 2 units down, 3 units left | 15. $y = - x $, $\frac{3}{5}$ unit up |

Write the equation of each translation of $y = x$ or $y = |x|$.



Each graph shows a translation of $y = -|x|$. State the values of h and k .



Graph each equation.

- | | | |
|-----------------------|---|------------------------|
| 22. $y = x - 1 + 2$ | 23. $y = -\left x + \frac{1}{2}\right $ | 24. $y = - x + 3 - 1$ |
| 25. $y = -x - 1 $ | 26. $y = - x - 2 + 4$ | 27. $y = x + 2 - 1$ |

